

**fifo+**<sup>11,40</sup>

for clients  $C$  sends FIFO

from  $j$  to  $i$  via  $(S[j,i], codes)$

receives at  $i$  via  $(R[i], decodes)$  requests  $Req[j]$  are acknowledged by  $Ack[j,i]$

$$\begin{aligned} &\equiv_{\text{def}} \forall i:C. \\ &\exists f:\{e:E \mid R(i,e)\} \rightarrow \{e:E \mid \exists j:C. (S(j,i,e))\} \\ &\quad (\lambda e.\exists j:C. (S(j,i,e)) \leftarrow\leftarrow f \dashv\vdash \lambda e.R(i,e) \\ &\quad \& (\forall e:\{e:E \mid R(i,e)\}, j:\{j:C \mid S(j,i,f(e))\}. \\ &\quad \quad decodes(i,e, \text{state when } e) = codes(j,i,f(e), \text{state when } f(e))) \\ &\quad \& (\forall e, e':\{e:E \mid R(i,e)\}, j:C. \\ &\quad \quad (S(j,i,f(e)) \Rightarrow (S(j,i,f(e')) \Rightarrow f(e) \text{ c}\leq f(e') \Rightarrow e \text{ c}\leq e') \\ &\quad \& (\forall j:C. \\ &\quad \quad \exists req:\{e:E \mid Ack(j,i,e)\} \rightarrow \{e:E \mid S(j,i,e) \& Req(j,e)\} \\ &\quad \quad (\lambda e.S(j,i,e) \& Req(j,e) \leftarrow\leftarrow req \dashv\vdash \lambda e.Ack(j,i,e) \\ &\quad \quad \& (\forall a:\{e:E \mid Ack(j,i,e)\}. \exists e:\{e:E \mid R(i,e)\}. (f(e) = req(a) \& e \text{ c}\leq a) \\ &\quad \quad \& e.req(e) \text{ is c}\prec \text{ preserving on } e.Ack(j,i,e)))) \end{aligned}$$

*clarification:*

**fifo+** $(es; codes; decodes; C; S; R; T; Req; Ack)$

$$\begin{aligned} &\equiv_{\text{def}} \forall i:C. \\ &\exists f:\{e:es-E(es) \mid R(i,e)\} \rightarrow \{e:es-E(es) \mid \exists j:C. (S(j,i,e))\} \\ &\quad (\text{antecedent-surjection}(es; \lambda e.R(i,e); \lambda e.\exists j:C. (S(j,i,e)); f) \\ &\quad \& (\forall e:\{e:es-E(es) \mid R(i,e)\}, j:\{j:C \mid S(j,i,f(e))\}. \\ &\quad \quad decodes(i,e, \text{es-state-when}(es;e)) = codes(j,i,f(e), \text{es-state-when}(es;f(e))) \in T) \\ &\quad \& (\forall e:\{e:es-E(es) \mid R(i,e)\}, e':\{e:es-E(es) \mid R(i,e)\}, j:C. \\ &\quad \quad (S(j,i,f(e)) \\ &\quad \quad \Rightarrow (S(j,i,f(e')) \\ &\quad \quad \Rightarrow \text{es-causle}(es;f(e);f(e')) \\ &\quad \quad \Rightarrow \text{es-causle}(es;e;e')) \\ &\quad \& (\forall j:C. \\ &\quad \quad \exists req:\{e:es-E(es) \mid Ack(j,i,e)\} \rightarrow \{e:es-E(es) \mid S(j,i,e) \& Req(j,e)\} \\ &\quad \quad (\text{antecedent-surjection}(es; \lambda e.Ack(j,i,e); \lambda e.S(j,i,e) \& Req(j,e); req) \\ &\quad \quad \& (\forall a:\{e:es-E(es) \mid Ack(j,i,e)\}. \\ &\quad \quad \quad \exists e:\{e:es-E(es) \mid R(i,e)\}. (f(e) = req(a) \in \text{es-E}(es) \& \text{es-causle}(es;e;a)) \\ &\quad \quad \& \text{causal-order-preserving}(es;e.req(e); e.Ack(j,i,e)))) \end{aligned}$$